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Abstract. Electrodynamic properties of fluorine-doped tin oxide films grown by aqueous-spray-based heterogeneous reaction on heated hydrophilic substrates were investigated with emphasis on applications to infrared plasmonics. These properties were correlated with physical ones such as crystallinity, dopant and electron concentrations, conductivity, and mobility. The degree of crystallinity for the nanocrystalline films increases with F concentration and growth temperature. The F concentration in the films is proportional to that in the starting solution. Electron concentration and Hall mobility rise more slowly with F concentration. At their highest, both F and electron concentrations are ~2% of the Sn concentration. In more lightly doped films, the electron concentration significantly exceeds the F concentration. The achieved resistivity of the doped films is lower than for undoped SnO$_2$ film by 20 to 750 times. The infrared complex permittivity spectrum shows a shift in plasma frequency at which the real part of the permittivity passes zero. The latter properties may interact in a complex way. Thus, for plasmonic applications, it is important to investigate electrodynamic, transport, and physical properties simultaneously as a function of growth conditions and dopant concentration.

1 Introduction

Fluorine-doped tin oxide (F:SnO$_2$ or FTO) has demonstrated value as a transparent conducting oxide in solar cells. It has been suggested as a heat-absorbing coating for window glass. More recently, FTO has been investigated as a host for surface plasmon polaritons (SPPs) in proposed infrared plasmonic devices.

SnO$_2$ is a wide band-gap semiconductor with natural n-type conductivity due to oxygen vacancies and interstitial Sn. Since tin exists in the lattice as an ion with charge 4+$\cdot$8 Each oxygen atom in the chemical formula accepts two electrons from Sn. Thus, each oxygen vacancy may result in two free electrons.

Doping with fluorine is known to increase conductivity, allowing F:SnO$_2$ to be used in electronic devices. Fluorine dopants are initially expected to fill oxygen vacancies, which relieves the surrounding lattice distortion. Thus, low-level fluorine doping may actually decrease free-electron density because two free electrons of the vacancy are reduced to one, due to the reception of the other electron by the fluorine to complete the bond. At higher concentrations, F may replace O in the lattice, causing an increase in the carrier concentration. The highest fluorine concentrations may include interstitial fluorine, which is an electron acceptor that would decrease the free-electron density, as has been observed. In any case, the electron concentration might be a complicated function of fluorine dopant concentration that depends on the conditions of growth and doping.

SPP properties depend on the frequency-dependent complex permittivity, which depends not only on carrier concentration but also on relaxation time (in the Drude model) and on other loss processes in general. The latter properties may depend on physical characteristics such as crystallinity. All relevant quantities may interact in a complex way. Thus, for plasmonic applications, it is important to investigate electrodynamic, transport, and physical properties simultaneously as a function of growth conditions and dopant concentration.

Fluorine doping is a means of controlling conductivity, which is necessary for many optoelectronic applications. Specifically, in the case of plasmonics, the free-carrier concentration and mobility have much to do with confinement and propagation of SPPs, which are inhomogeneous electromagnetic waves bound to the surface of a conductor. The frequency at which the real part of the permittivity $\varepsilon'$ passes from positive to negative values can be considered to represent the transition point from dielectric to metallic optical behavior. The latter is required to sustain an SPP. The “dressed” plasma frequency is often defined as the frequency corresponding to this zero-crossing frequency. At lower frequencies, the material is able to support SPPs, where such material may find application in proposed plasmonic devices.

Although an investigation of SPPs on transparent conducting oxides (TCO) can be found as far back as 1990, interest and activity in TCOs for plasmonics has accelerated strongly within the last decade. Specific TCO-based plasmonic devices have included on-chip waveguides,
absorbers,\textsuperscript{20,21} filters,\textsuperscript{22} and modulators.\textsuperscript{23} The plasmonic TCOs investigated so far are predominantly indium tin oxide and gallium- or aluminum-doped zinc oxide.\textsuperscript{24,25} More comprehensive reviews on plasmonic materials can be found in the literature.\textsuperscript{24-26} Plasmonic applications could benefit from low-cost large area deposition of an environmentally friendly inexpensive material such as FTO.

Many approaches to fabrication of FTO have been reported, including pulsed laser deposition,\textsuperscript{27} sol–gel,\textsuperscript{28} sputtering,\textsuperscript{11,12} sintered powders,\textsuperscript{29} and chemical bath deposition.\textsuperscript{30} Our absorbers,\textsuperscript{20,21} filters,\textsuperscript{22} and modulators.\textsuperscript{23} The plasmonic precursors comprised 0.4 M stannic chloride (SnCl\textsubscript{4}·2H\textsubscript{2}O) to serve as nucleation sites. The organic solvents ethanol, isopropanol, and methyl propanol serve as the source of the surface-attached hydroxyl ions to serve as nucleation sites. The perfect conformity is important because many plasmonic applications require structured devices, such as slot waveguides,\textsuperscript{31,32} transmission gratings,\textsuperscript{33} and lamellar gratings.\textsuperscript{6}

There have been several other studies of aqueous spray deposition of FTO with similar chemistry and conditions.\textsuperscript{15,34-36} These studies of electrolytic properties relevant to transparent plasmonic applications, which is the emphasis of this paper. An objective of this study is to determine the range over which the plasma frequency can be tuned by fluoride doping and growth conditions. The plasma frequency is important to plasmonic applications because SPP fields are most tightly bound when their frequency is close to it.

2 Experimental Details

FTO films were grown on hydrophilic substrates by stream deposition for electrodeless electrochemical deposition (SPEED) at atmospheric pressure.\textsuperscript{7} In contrast to chemical bath deposition, SPEED ensures that films grow by heterogeneous reaction on the surface rather than in solution. Precursors comprised 0.4 M stannic chloride (SnCl\textsubscript{4}·2H\textsubscript{2}O) and ammonium fluoride (NH\textsubscript{4}F) dissolved in a mixture of deionized water and organic solvents. Water (20% by volume) acts as a solvent, as the source of the surface-attached OH\textsuperscript{−} nucleation sites for heterogeneous reaction, and as the source of oxygen. The organic solvents ethanol, isopropanol, and methyl propanol serve as complexing agents for Sn ions.

For convenience, we chose silicate glass surfaces on which to grow films since these hydrophilic surfaces attach hydroxyl ions to serve as nucleation sites. The OH\textsuperscript{−} ions attract positively charged complexes to initiate the electrochemical reaction, without external electrical field or electrodes. The heterogeneous chemical reactions are

\[
\text{[Sub]}\text{OH}^- + \text{[SnL}^n]\overset{p+1\pm}{\longrightarrow} \text{[Sub]}\text{Sn(OH)}^\pm + (\text{L}_n)^p \downarrow, \tag{1}
\]

\[
\text{[Sub]}\text{Sn(OH)}^{3+} + 3\text{OH}^- \rightarrow \text{[Sub]}\text{SnO}_2 + 2\text{H}_2\text{O} \uparrow, \tag{2}
\]

where L is the ligand supplied by the organic solvents, [Sub] is the heated substrate, p is the charge of the ligand L, and n is the number of ligands involved in the Sn/L coordination. Up arrows indicate decomposition and evaporation of reaction byproducts. Substrate temperature must exceed the heterogeneous reaction activation energy and be sufficient to eliminate byproducts. Site regeneration follows:

\[
\text{[Sub]}\text{SnO}_2 + \text{OH}^- \rightarrow \text{[Sub]}\text{SnO}_2(\text{OH})^- . \tag{3}
\]

The freshly attached OH\textsuperscript{−} initiates the next growth cycle. Lateral grain growth competition leads to nanoparticle morphology. Fluorine doping follows:

\[
\text{[Sub]}\text{Sn(OH)}^{3+} + 4\text{NH}_4\text{F} + 3\text{OH}^- \rightarrow \text{[Sub]}\text{SnF}_4 + 4\text{H}_2\text{O} \uparrow + 4\text{NH}_3 \uparrow . \tag{4}
\]

Oxygen vacancies occur via adsorption of the tin complex \([\text{SnL}_n]^{p+1\pm}\) according to

\[
\text{[Sub]}\text{Sn(OH)}^{3+} + m\text{OH}^- \rightarrow \text{[Sub]}\text{Sn} + m\text{OHL}_n \uparrow. \tag{5}
\]

We already demonstrated good nanocrystalline films with plasma wavelength near 2 μm using 20% F/Sn precursor ratio at growth temperatures near \(\sim 500^\circ\text{C}\).\textsuperscript{6} We began this study with a coarse sampling that spanned a wide range of F concentrations at the more moderate temperature \(450^\circ\text{C}\) using borofloat glass substrates. Results presented below suggest the need for higher temperatures, so a second set of samples was processed at \(480^\circ\text{C}\), but with finer sampling of the F concentration. Results for this group suggested that even higher temperatures would increase the achieved conductivity. To achieve higher surface temperatures for the same \(480^\circ\text{C}\) hot plate temperature, we turned to thinner substrates with higher thermal conductivity, namely silicon, on which a thin hydrophilic SiO\textsubscript{2} layer was first deposited. Silicon substrate is also advantageous with respect to CMOS compatibility. The investigation with silicon substrates focused on the highest doping to achieve the highest conductivity near the limiting temperature of our growth apparatus. All temperatures refer to hot plate temperatures. Measurement of substrate surface temperature would be preferred, but this is impractical. Contact thermometry disturbs the film growth. Infrared thermometry is hampered by poor knowledge of the emissivity and by obscuring clouds of steam during deposition.

Table 1 presents the list of the samples prepared and studied for this paper, along with growth temperature, substrate, and nominal fluorine concentration. The latter is the concentration in the precursor solution. The hot-plate exceeds the actual growth temperatures due to imperfect thermal coupling, finite substrate thermal conductivity, and evaporative cooling at the surface. Precursor solutions were mixed with targeted fluorine concentrations. The flow rate through the spray nozzle was set using a manual valve. When changing between solutions with different concentrations, the valve was closed, all lines were cleaned, and the valve was reset to the original position for spraying the next film.

Asymmetric out-of-plane x-ray diffraction (XRD) was performed at fixed \(\omega = 10^\circ\text{deg}\) incidence using a Cu x-ray mirror with a 1/32-deg divergence slit and a 0.04-rad soller slit on the incident beam. The divergent beam also had a 0.04-soller slit and was measured on a PIXcel detector comprising a 255 × 255 array. All detectors were used in a scanning line mode to integrate the signal across each line for a cumulative dwell time of 20.4 s per 0.05 deg step over a 2θ range of 10 deg to 90 deg.

Vertical concentration profiles of Sn, O, F, and Cl were determined using secondary ion mass spectroscopy (Physical
Table 1 FTO samples.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Hot plate temperature (°C)</th>
<th>Substrate</th>
<th>Nominal F/Sn ratio (%)</th>
</tr>
</thead>
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<tr>
<td>A0.5</td>
<td>450</td>
<td>Glass</td>
<td>0.5</td>
</tr>
<tr>
<td>A5</td>
<td>450</td>
<td>Glass</td>
<td>5</td>
</tr>
<tr>
<td>A15</td>
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<td>Glass</td>
<td>15</td>
</tr>
<tr>
<td>B0.1</td>
<td>480</td>
<td>Glass</td>
<td>0.1</td>
</tr>
<tr>
<td>B0.2</td>
<td>480</td>
<td>Glass</td>
<td>0.2</td>
</tr>
<tr>
<td>B0.5</td>
<td>480</td>
<td>Glass</td>
<td>0.5</td>
</tr>
<tr>
<td>B1</td>
<td>480</td>
<td>Glass</td>
<td>1</td>
</tr>
<tr>
<td>B2</td>
<td>480</td>
<td>Glass</td>
<td>2</td>
</tr>
<tr>
<td>B5</td>
<td>480</td>
<td>Glass</td>
<td>5</td>
</tr>
<tr>
<td>B10</td>
<td>480</td>
<td>Glass</td>
<td>10</td>
</tr>
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<td>B20</td>
<td>480</td>
<td>Glass</td>
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<tr>
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</tr>
<tr>
<td>C20</td>
<td>480</td>
<td>Si/SiO₂</td>
<td>20</td>
</tr>
</tbody>
</table>

Electronics ADEPT 1010 quadrupole SIMS). The primary 3 keV Cs⁺ ions were rastered over a 300 μm × 300 μm area at 45 deg incidence with beam current 20 nA. To reduce the crater side wall effects, a 20% electronic gating was used to collect the ejected ions from just the center region. For the calibration standard, fluorine ions were implanted into an undoped SPEED-grown SnO₂ film at 180 keV energy and ion dose of 5.626 × 10¹⁵ cm⁻² (Leonard Kroko, Inc.). A sputtering rate of 0.636 nm/s was determined for the implanted standard by crater-depth profilometry. This rate was assumed to hold for the other films when deducing their thicknesses from the SIMS depth profiles. A relative sensitivity factor (RSF) value of 5.58 × 10¹⁸ atoms/cm³ was determined from the implant dose and the sputtering rate using SIMetric (the instrument control program), whose three cursors on the interactive display define integration limits and background. Recorded intensities for fluorine \( I_F \) were normalized to the Sn intensity \( I_{Sn} \) from the matrix, and the fluorine concentration [F] of the SPEED-grown films was determined according to \( [F] = \text{RSF}(I_F/I_{Sn}) \). SRIM/TRIM simulation indicates that the dopant concentration peak (ion range) occurs at depth 206.1 nm, but SIMS data for the implanted standard find the peak at a depth of 237 nm, where the peak fluorine concentration was determined to be 3.111 × 10¹⁰ cm⁻³. The SnO₂ concentration was calculated from the mass density 6.95 g/cm³ to be 2.77 × 10²³ cm⁻³, so the peak F/Sn ratio in the standard was 1.12%. Sample thicknesses were determined using cross-sectional imaging with a scanning electron microscope (SEM). SEM images of typical polycrystalline FTO surfaces have been published.⁵,⁶ Contactless rf-eddy-current method (Lehighton Electronics, Inc.) was used to map sheet resistance \( R_s \), whose values were also determined by a four-point probe method. Resistivity \( \rho \) was found by multiplying \( R_s \) and film thickness.

Hall effect measurements were completed using an Accent Optical Technologies system in the Van der Pauw configuration. The magnetic field strength was 4.86 kG with the current fixed for each film measurement. The measurements were used to determine carrier type, carrier concentration \( n \), and mobility \( \mu \). Resistivity from Hall data was determined according to \( \rho = 1/(ne\mu) \), where \( e \) is the electron charge.

All films were characterized over the 2- to 15-μm wavelength range using a J.A. Woollam IR-VASE infrared ellipsometer. For each set of samples, the substrates were first characterized and their complex permittivity spectra used in the subsequent film analysis. Complex optical constants were fitted to a single layer with thicknesses determined by SEM. This method is not necessarily Kramers–Kronig consistent, but it prevents loss of small features such as those observed in the 6- to 9 μm range, and it retains a measure of the noise. As a check, the layer was also modeled using Kramers–Kronig consistent oscillators; practically the same optical constants were obtained, but the fine details were lost. Ellipsometry performed at one of the center of each film, where a SEM cross section was used to determine the film thickness.

Transmittance spectra \( T \) over wavelengths from UV to near-IR were collected using a PerkinElmer Lambda 900 spectrometer at ambient conditions. The useful wavelength range was 200 nm to 2.5 μm at 2-nm resolution. A spectrum of uncoated borofloat glass was used as reference. Film thicknesses \( d = 1/(2n\Delta) \) were determined from the average fringe separation in wavenumbers \( \Delta \) using \( n = 2.006 \) as the index value for SnO₂.

3 Results

Figure 1 shows XRD data for sample sets A, B, and C. Samples A show a broad band at low angles due to the glass substrate. The A samples have no distinct peaks, and only at the highest concentration do some weak broad peaks begin to appear at 53 deg and 64 deg, which are near to the positions of the (211) and (221) peaks for SnO₂. There is only the barest suggestion of a sharp (200) peak in sample A15. Thus, the A samples appear to be poorly crystallized.

Only a selection of the XRD data for the B sample set is presented, but all samples were so characterized. These films show distinct peaks of tetragonal SnO₂, class \( D_{4h} \), space group \( P4_{2} /mmm \) on top of the broad substrate band. The 30 deg higher growth temperature compared to A samples evidently improved the crystallinity, but this also apparently depends on the F concentration. The (110) peak of SnO₂ is observed only for sample B20.
For samples C, the glass feature is missing and no Si peaks were observed. The (110), (101), (200), (211), (221), (301), and (321) peaks are identified by symbols and labeled (PDF# 000-041-1445). No additional peaks were observed, and the observed lines do not match the reference data for other tin oxides, such as SnO or Sn$_3$O$_4$. The C samples are clearly more crystalline than the other two groups, which we attribute to high growth temperature on the more thermally conducting Si substrates. As for the B samples, the peak heights depend on F concentration.

The XRD peak strengths depend systematically on F/Sn ratio. Figure 2 presents the (200) peak height versus nominal [F] concentration for samples B and C. The values have been normalized to the maximum value within each sample set. Except for the highest concentration B sample, the peak intensity increases monotonically with nominal F:Sn ratio, suggesting increased crystallinity with [F]. The observed peak-strength differences cannot be explained in terms of differences in film thickness. As will be shown below, the thickness of the B samples varies nonmonotonically with nominal F:Sn ratio, while the change in thickness for C samples (monotonic in SEM data, but nonmonotonic in SIMS data) is by only a factor of 1.2. The decrease in XRD peak strength at the highest F concentration for B samples might be due to the accumulation of fluorine at interstitial lattice sites, which should deform the lattice. That such a decrease does not occur in the C series may be due to the effectively higher surface temperature during growth (if higher temperature favors substitutional over interstitial positions.)

The full widths at half maximum $\beta$ of the dominant (200) peak are 0.5 deg and 0.25 deg for samples B and C, respectively, independent of [F]. The Scherrer equation gives a lower bound for the mean size of ordered crystalline domains $\tau = K\lambda / \beta \cos \theta$, where $K \sim 0.9$ is the shape factor, $\lambda = 0.15418$ nm Cu K-alpha wavelength, $\beta$ is in radians, and the Bragg angle $\theta$ is 19 deg. For sample sets B and C, we find the crystalline domains to be not smaller than $\tau = 10$ and 20 nm, respectively. The higher surface temperature during growth for samples C unsurprisingly tends to favor a higher degree of crystallinity and larger crystallite size.

Figure 3 presents a plot of the actual F/Sn ratio determined from the analysis of SIMS data for all three sample sets as a function of the ratio in the starting solution. The dashed line with unity slope shows that the achieved F concentration is proportional to the amount added to the solution but lower by a factor of $\sim 30$. The values for C samples tend to lie above the line through the values for the B samples. The values for the A samples fall below. Thus, higher growth temperature tends to favor fluorine incorporation into the lattice. The fluorine concentration was observed to be fairly uniform throughout the film thickness for most of the samples.

As an independent confirmation of the SIMS concentration values, sample B20 was measured by x-ray photoelectron spectroscopy (XPS). The fluorine peak was very weak, but long averaging allowed us to determine a fluorine concentration of $\sim 0.65\%$. This value is close to the value 0.46% for the data point shown in Fig. 3. From XRD data, sample B20 appears to be an outlier, which has been tentatively attributed to lattice deformation caused by an accumulation of interstitial fluorine. However, XPS at this level of signal-to-noise ratio is insensitive to the deformation of the lattice or...
to the positions of F atoms, so it remains a useful check on the SIMS values. This most heavily doped B sample was the only one that gave sufficiently strong XPS signal to quantify its fluorine concentration with any confidence. C samples were not investigated by XPS.

Figure 4 presents a sheet resistance map determined by the contactless method for sample C20. The contours are correlated with the positions of the clips used to hold the substrate in contact with the hot plate during growth. This again shows the importance of substrate temperature on film properties. The average value is 14.6 Ω/sq with 12% systematic spatial variation over the 5-cm lateral dimension of the film. A similar measurement on sample A15 shows twice higher spatial variations, which is attributed to lower temperature uniformity during growth on the thrice thicker, 130×-less-thermally conductive glass substrate.

Figure 5 presents plots of film thickness, resistivity, Hall mobility, and electron concentration as a function of fluorine concentration. Thicknesses determined from SEM imaging and SIMS profiling are presented first in Fig. 5. The SEM and SIMS values are in good agreement. The C samples are more than twice as thick as the A and B samples for the same [F]. We interpret this to be a consequence of the higher growth temperature on Si substrates due to higher thermal conductivity.

Next, Fig. 5 shows resistivity versus [F]. SEM thickness values were used to determine the plotted values. Hall, contactless, and four-point probe values are in good agreement. Samples A have the highest resistivity, and the values decrease with increasing nominal [F]. For samples B, a 200-fold [F] increase varies the resistivity by only a factor of ~10, and this variation is systematic but nonmonotonic. Set C has overall lower resistivity, with lowest value achieved at [F] = 15%.

The Hall values of mobility μ and electron concentration n are also plotted in Fig. 5 for samples B and C. For B samples, n varies only by a factor of 3.3, while μ varies by a factor of 3.0, so both factors contribute nearly equally to the observed 10-fold variation in resistivity. Since the mobility values for B and C samples are about the same, their difference in resistivity value is due mainly to their different electron concentrations. The electron and actual fluorine concentrations in sample C20 are 5.9 × 10²⁰ cm⁻³ and 5.1 × 10²⁰ cm⁻³, a difference of only 14%, which is comparable to the level of uncertainty for [F] values from SIMS. A similar situation holds for sample B10. This suggests that a substantial portion of F dopant ions in SPEED-grown films can be electrically active. On the other hand, with decreasing [F], the electron concentration does not drop proportionally. For the lowest doped sample, [e⁻] > [F] by a factor of ~60, which suggests an additional source of free carriers, possibly oxygen-vacancy double-donors. The resistivity of the undoped SnO₂ film before ion-implantation was determined by 4-pt probe to be 0.6 Ω-cm, which is a factor 20 to 750 higher than for the F-doped samples shown in Fig. 5. That means that the doping process during SPEED growth is responsible for all of the additional charge carriers, even if they cannot all be accounted for by the concentration of F.

Interestingly, the implanted standard prepared for SIMS had a resistivity of 6 Ω-cm, i.e., 10x higher than that of the undoped SnO₂ film before implantation. This suggests that implant damage substantially worsens the electron mobility and that the implanted F ions are not all electrically active. Thus, ion implantation is a poor approach to preparing FTO, unless a suitable annealing process can be developed to heal the damage and activate the dopants. In any case, SPEED has the practical advantage over implantation of being a low-cost, large-area fabrication process.

Figure 6 presents real and imaginary parts of the SnO₂:F permittivity spectra in the infrared wavelength range 2 to 15 µm for different F concentrations (sample set B). The magnitudes of both parts of the permittivity are similar. The ε'' increases, and ε' becomes more negative, with increasing F concentration up to 10%, after which the change...
reverses. The zero crossings of $\varepsilon''$ shift to shorter wavelength up to $\frac{1}{2} F/C_{138} \approx 10\%$, after which it stops changing. There is structure in the 6- to 10-$\mu$m range. This is not due to the known IR-active phonon bands of SnO$_2$ (three of $\text{Eu}$ type and one of $\text{A}_2\text{u}$), which fall in the wavelength range 14 to 41 $\mu$m.\(^{38-41}\) Note particularly the broad peak in $\varepsilon''$ at $\sim 9.4$ $\mu$m, which is similar to the well-known 9-$\mu$m absorption band in silicates.\(^{42}\) This band becomes weaker with increasing $[F]$. In A samples grown at 450°C, the overall $\varepsilon''$ curves have lower value, and the 9.4-$\mu$m peak is much stronger while retaining the same weakening trend with increasing $[F]$.

Figure 7 presents plots of the $\varepsilon'$ zero-crossing wavelength for the three sample sets (labeled) and also a single data point from the literature.\(^6\) The A samples are metallic only at the highest fluorine concentrations, and then they behave optically as conductors only beyond 13 $\mu$m wavelength. The B and C samples have $\varepsilon'$ zero-crossings throughout the mid-wave IR (3 to 5 $\mu$m) to long-wave IR (8 to 12 $\mu$m) for all values of F doping studied. At low doping values, the zero-crossings are all about 14 to 15 $\mu$m wavelength. At $[F] \sim 1\%$, the zero-crossing wavelength drops rapidly with increasing concentration until about 5% F, when the value stops changing and remains at about 2 to 3 $\mu$m. Though the changes with $[F]$ in Fig. 6 spectra reverse above 10%, the zero crossings do not. The high-concentration zero-crossing wavelengths for samples B exceed those for samples C by a factor of $\sim 1.5$.

There may well be plasmonic applications such as structured plasmonic resonators that provide wavelength-specific infrared or microwave absorption simultaneously with visible and near-IR transparency. Figure 8 presents examples of UV-visible transmittance spectra of A and B films that confirm such transparency. (The silicon substrates of C films are opaque in this wavelength range.) All A and B films were so characterized and all show similar features. These include fundamental absorption at around 300 nm wavelength (4.1 eV), high transmittance at longer wavelengths, and oscillations due to Fabry–Perot resonances in the films. The latter arise because the SnO$_2$ index ($n \sim 2.006$) differs significantly from that of air (1) and borofloat glass (1.47). Film thicknesses determined from the fringes agree with the values plotted in Fig. 5. The longest wavelength transmission decreases within increasing conductivity. For the highest conductivity samples, this down turn happens near the plasma wavelength where the transition from dielectric to metallic optical behavior begins.

4 Discussion

Figure 4 shows the importance of temperature uniformity in obtaining uniform electrical properties of the film. Silicon has more than two orders of magnitude higher thermal conductivity than borofloat glass, and the Si substrates were three times thinner, so the surface temperature should be higher for the C samples. The elevated temperatures volatize and eliminate reaction byproducts that impair conductivity, so C films are expected to have higher quality and higher uniformity. We observe the C samples to be more crystalline, with larger crystallite size, higher electron concentration, and lower resistivity.

The thickness oscillations with changes in F concentration are difficult to understand, but the observed nonrandom behavior suggests either a physical interaction or a systematic error due to some uncontrolled environmental factor for samples processed in order of increasing concentration. If the variations were due to uncertainties in the positioning of the manual value on the spray system, one would expect a more random variation in thickness.
For sample B0.1, the actual fluorine concentration is $1.8 \times 10^{18}$ cm$^{-3}$, while the free-electron concentration $n = 1.1 \times 10^{20}$ cm$^{-3}$. In undoped SnO$_2$ grown by SPEED, $n_0 = 5.5 \times 10^{19}$ cm$^{-3}$, assuming its higher resistivity is due mainly to lower free-electron density. These values are inconsistent with a model in which F dopants initially fill oxygen vacancies, replacing those double donors by F single donors and thereby reducing $n_0$. For each F ion in this sample, there are an additional 60 free electrons compared with the undoped SnO$_2$. Thus, the very process of F doping in SPEED is introducing electrically active defects far above the actual number of dopant impurities. In contrast, at the highest doping levels, $n \sim [F]$, so all free electrons can be accounted for if the majority of fluorine ions replace oxygen ions in the lattice.

Similar to Ref. 15, we see a minimum in FTO resistivity at $[F] = 15\%$. However, in contrast to Ref. 15, we do not see a minimum in $\mu$ or a maximum in $n$ at this concentration. Rather we observe a monotonic change in $n$ from 10% to 20%, and a maximum in $\mu$. Thus, our resistivity valley at 15% is due to our mobility peak, not a concentration peak. Reference 13 also reported that the highest concentration of 20%, and a maximum in $n_0$. For each F ion in this sample, there are an additional 60 free electrons compared with the undoped SnO$_2$. Thus, the very process of F doping in SPEED is introducing electrically active defects far above the actual number of dopant impurities. In contrast, at the highest doping levels, $n \sim [F]$, so all free electrons can be accounted for if the majority of fluorine ions replace oxygen ions in the lattice.

The main objective of this study was to investigate the range over which the plasma frequency could be tuned by fluorine doping and growth conditions. We summarize that we achieved plasma wavelengths from beyond 14 $\mu$m to below 2 $\mu$m. In other words, obtaining plasma frequencies anywhere in the important midwave and long-wave infrared bands was shown to be possible. It is clearly possible to obtain even longer plasma wavelengths into the far-IR and mm-wave regions with FTO, but apparently it would be difficult to go much below 2 $\mu$m in the near-infrared. However, there are many other materials well suited for that range.

## 5 Conclusion

In conclusion, electrode dynamic properties of fluorine-doped tin oxide films grown by aqueous spray deposition were correlated with physical and electrical properties over a broad range of doping concentrations. Results indicate that the substantial reduction in resistivity of doped films with respect to undoped SnO$_2$ results from a complex mechanism of free-electron generation, which depends on the doping process but is not simply accounted for by the density of dopants. Crystallinity, mobility, and carrier concentration all have complicated dependence on dopant concentration and surface temperature during growth. The results presented here especially inform the tailoring of electrode dynamic properties in aqueous-spray grown FTO for application to infrared plasmonics.

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