

Name: Key

PHY2054.002, Fall 2010

Exam #1

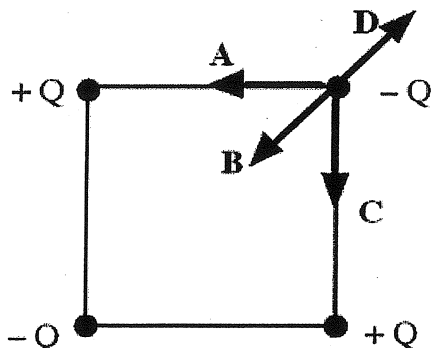
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Version A

Part I (60%)

B

1. Four point charges, each of the same magnitude, with varying signs are arranged at the corners of a square as shown. Which of the arrows labeled A, B, C, and D gives the correct direction of the net force that acts on the charge at the upper right corner?



- A) A, B) B, C) C, D) D, E) The net force on that charge is zero.

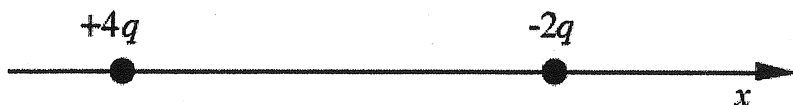
A

2. Two positive point charges  $Q$  and  $2Q$  are separated by a distance  $R$ . If the charge  $Q$  experiences a force of magnitude  $F$  when the separation is  $R$ , what is the magnitude of the force on the charge  $2Q$  when the separation is  $2R$ ?

- A)  $F/4$ , B)  $F/2$ , C)  $F$ , D)  $2F$ , E)  $4F$

C

3. At which point (or points) is the electric field zero N/C for the two point charges shown on the  $x$  axis?



- A) The electric field is never zero in the vicinity of these charges. B) The electric field is zero somewhere on the  $x$  axis to the left of the  $+4q$  charge. C) The electric field is zero somewhere on the  $x$  axis to the right of the  $-2q$  charge. D) The electric field is zero somewhere on the  $x$  axis between the two charges, but this point is nearer to the  $-2q$  charge. E) The electric field is zero at two points along the  $x$  axis; one such point is to the right of the  $-2q$  charge and the other is to the left of the  $+4q$  charge.

E

4. Which one of the following statements is true concerning the strength of the electric field between two oppositely charged parallel plates?

- A) It is zero midway between the plates. B) It is a maximum midway between the plates. C) It is a maximum near the positively charged plate. D) It is a maximum near the negatively charged plate. E) It is constant between the plates except near the edges.

A

5. What is the electric flux passing through a Gaussian surface that surrounds a  $+0.075 \text{ C}$  point charge?

- A)  $8.5 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}$ , B)  $6.8 \times 10^8 \text{ N}\cdot\text{m}^2/\text{C}$ , C)  $1.3 \times 10^7 \text{ N}\cdot\text{m}^2/\text{C}$ , D)  $4.9 \times 10^6 \text{ N}\cdot\text{m}^2/\text{C}$   
E)  $7.2 \times 10^5 \text{ N}\cdot\text{m}^2/\text{C}$

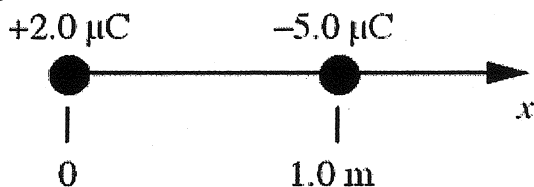
D

6. The electric potential at a certain point in space is  $12 \text{ V}$ . What is the electric potential energy of a  $-3.0 \mu\text{C}$  charge placed at that point?

- A)  $+4 \mu\text{J}$ , B)  $-4 \mu\text{J}$ , C)  $+36 \mu\text{J}$ , D)  $-36 \mu\text{J}$ , E) zero  $\mu\text{J}$

B

7. Two point charges are arranged along the  $x$  axis as shown in the figure. At which of the following values of  $x$  is the electric potential equal to zero? Note: At infinity, the electric potential is zero.



- A)  $+0.05 \text{ m}$ , B)  $+0.29 \text{ m}$ , C)  $+0.40 \text{ m}$ , D)  $+0.54 \text{ m}$ , E)  $+0.71 \text{ m}$

C

8. A parallel plate capacitor with plates of area  $A$  and plate separation  $d$  is charged so that the potential difference between its plates is  $V$ . If the capacitor is then isolated and its plate separation is decreased to  $d/2$ , what happens to the potential difference between the plates?

- A) The final potential difference is  $4V$ ., B) The final potential difference is  $2V$ ., C) The final potential difference is  $0.5V$ ., D) The final potential difference is  $0.25V$ ., E) The final potential difference is  $V$ .

D

9. The plates of a parallel plate capacitor each have an area of  $0.40 \text{ m}^2$  and are separated by a distance of  $0.02 \text{ m}$ . They are charged until the potential difference between the plates is  $3000 \text{ V}$ . The charged capacitor is then isolated. Determine the magnitude of the electric field between the capacitor plates.

- A)  $60 \text{ V/m}$ , B)  $120 \text{ V/m}$ , C)  $1.0 \times 10^5 \text{ V/m}$ , D)  $1.5 \times 10^5 \text{ V/m}$ , E)  $3.0 \times 10^5 \text{ V/m}$

E

10. A capacitor has a very large capacitance of  $10 \text{ F}$ . The capacitor is charged by placing a potential difference of  $2 \text{ V}$  between its plates. How much energy is stored in the capacitor?

- A)  $2000 \text{ J}$ , B)  $500 \text{ J}$ , C)  $100 \text{ J}$ , D)  $40 \text{ J}$ , E)  $20 \text{ J}$

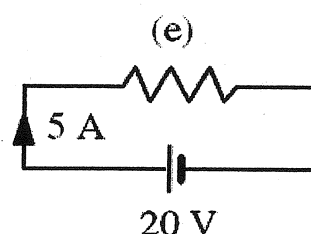
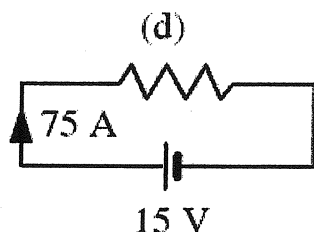
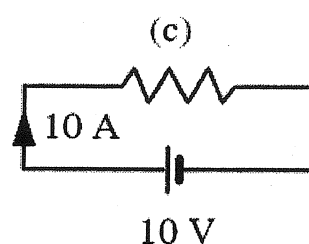
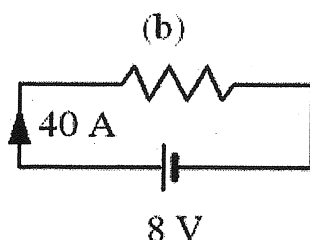
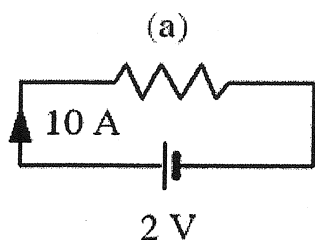
A

11. A  $3.5\text{-A}$  current is maintained in a simple circuit with a total resistance of  $1500 \Omega$ . What net charge passes through any point in the circuit during a thirty second interval?

- A)  $100 \text{ C}$ , B)  $180 \text{ C}$ , C)  $500 \text{ C}$ , D)  $600 \text{ C}$ , E)  $5200 \text{ C}$

E

12. Which one of the following circuits has the largest resistance?

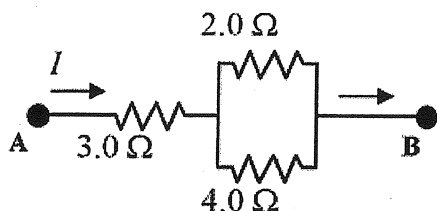


A) a, B) b, C) c, D) d, E) e

D

13. A 4-A current is maintained in a simple circuit with a total resistance of  $2\ \Omega$ . How much energy is delivered in forty five seconds?

- A) 720 J
- B) 96 J
- C) 360 J
- D) 1440 J
- E) 240 J



B

14. What is the equivalent resistance between the points A and B in figure above?

- A)  $3.8\ \Omega$ , B)  $4.3\ \Omega$ , C)  $5.1\ \Omega$ , D)  $6.8\ \Omega$ , E)  $9.0\ \Omega$

15. When two capacitors are connected in series, the equivalent capacitance of the combination is  $120\ \mu\text{F}$ . When the two are connected in parallel, however, the equivalent capacitance is  $480\ \mu\text{F}$ . What are the capacitances of the individual capacitors?

A

- A)  $240\ \mu\text{F}$  and  $240\ \mu\text{F}$ , B)  $125\ \mu\text{F}$  and  $325\ \mu\text{F}$ , C)  $175\ \mu\text{F}$  and  $275\ \mu\text{F}$ , D)  $150\ \mu\text{F}$  and  $300\ \mu\text{F}$ , E)  $80\ \mu\text{F}$  and  $370\ \mu\text{F}$

Part II (40%)

$$k = 9 \times 10^9 \frac{N \cdot m^2}{C^2}$$

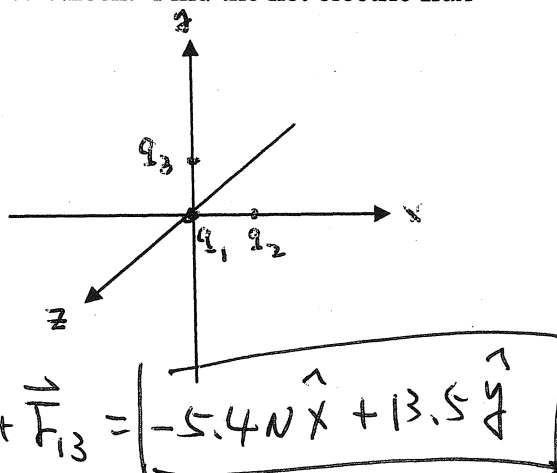
1. A charge  $q_1 = -3.0 \mu C$  is fixed at the origin. There are two more charges, one ( $q_2 = -2.0 \mu C$ ) is located at  $x=0.1 \text{ m}$ ,  $y=0$  and  $z=0$ , and the other ( $q_3 = +5.0 \mu C$ ) at  $x=0$ ,  $y=0.1 \text{ m}$ ,  $z=0$ . (a) Find the net electrostatic force acting on the charge at the origin? (10%) (b) Assume a Gaussian sphere with its center located at origin and its radius equals to  $0.25 \text{ m}$ . Find the net electric flux  $\Phi_E$  through this Gaussian surface. (5%)

$$(a) \vec{F}_{12} = -k \frac{(3 \times 10^{-6})(2 \times 10^{-6})}{(0.1)^2} \hat{x}$$

$$= -5.4 \text{ N } \hat{x}$$

$$\vec{F}_{13} = +k \frac{(3 \times 10^{-6})(5 \times 10^{-6})}{(0.1)^2} \hat{y}$$

$$= 13.5 \text{ N } \hat{y} \Rightarrow \vec{F}_{\text{net}} = \vec{F}_{12} + \vec{F}_{13} = \boxed{-5.4 \text{ N } \hat{x} + 13.5 \text{ N } \hat{y}}$$



$$(b) \Phi = \frac{Q_{\text{total}}}{\epsilon_0} = \frac{(-3 \mu C + -2 \mu C + 5 \mu C)}{\epsilon_0} = 0$$

2. A parallel plate capacitor with a capacitance of  $6 \mu F$  is charged with a  $12 \text{ Volts}$  battery until it is fully charged. Once it is fully charged, the battery is disconnected. The distance between the two plates is  $1.0 \text{ cm}$ . (a) Find the magnitude of the charge on each plate? (5%), (b) What is the electric field in the middle of the capacitor? (5%), (c) If a dielectric with  $\kappa = 2.5$  is filled the capacitor, what is the potential difference between the two plates of the capacitor? (5%)

$$d = 1.0 \text{ cm} \quad C = 6 \mu F \quad V = 12 \text{ Volt}$$

$$C = \frac{Q}{V}$$

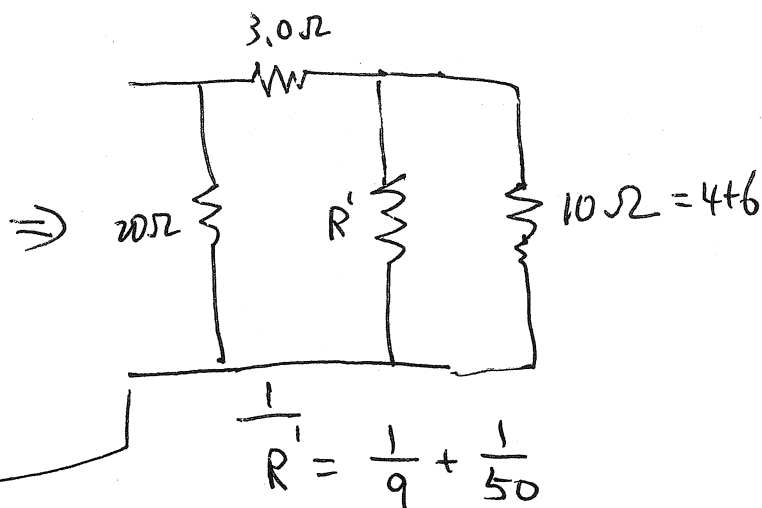
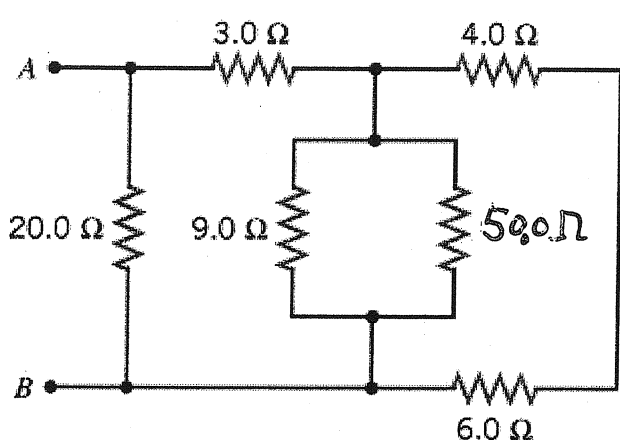
$$(a) Q = CV = \boxed{72 \mu C}$$

$$(b) |E| = \frac{\Delta V}{\Delta s} = \frac{12 \text{ Volt}}{0.01 \text{ m}} = \boxed{1200 \text{ V/m}}$$

$$(c) C' = \kappa C \quad C' = \frac{Q'}{V'} \quad \text{since } Q' = Q$$

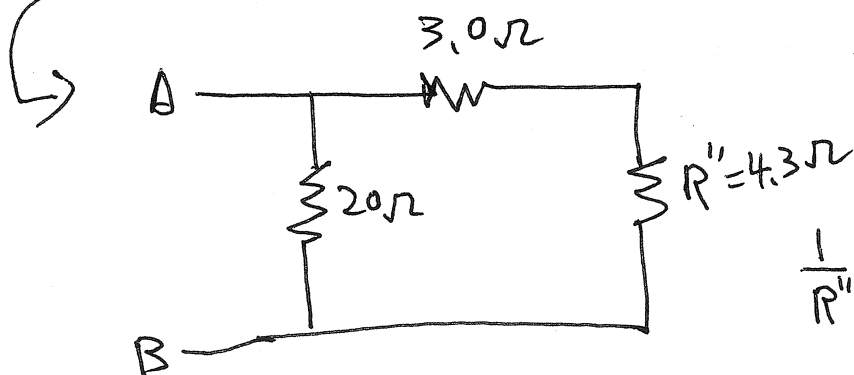
$$V' = \frac{12}{2.5} = \boxed{4.8 \text{ Volt}} \Rightarrow \boxed{V' = \frac{V}{\kappa}}$$

3. Determine the equivalent resistance between the points A and B for the group of resistors in the drawing.

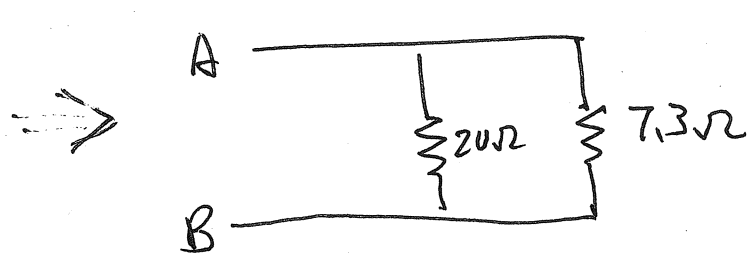


$$\frac{1}{R'} = \frac{1}{9} + \frac{1}{50}$$

$$R' = 7.6\ \Omega$$



$$\frac{1}{R''} = \frac{1}{7.6} + \frac{1}{10} \Rightarrow R'' = 4.3\ \Omega$$



$$\frac{1}{20} + \frac{1}{7.3} = \frac{1}{R'''}.$$

$$R''' = 5.35\ \Omega$$

