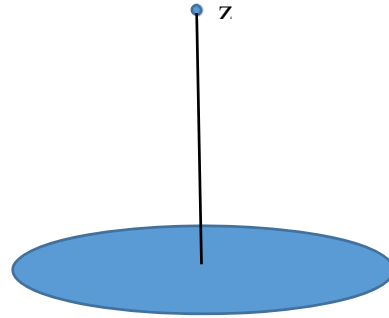
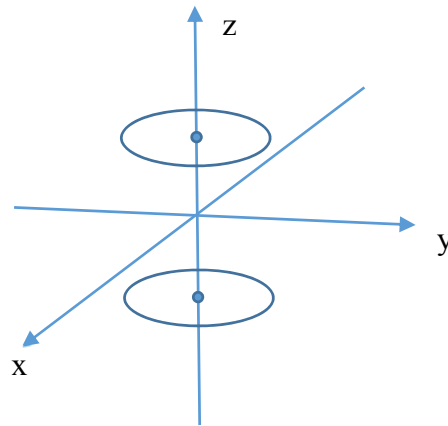


**Electricity & Magnetism I, Homework #9**  
**Fall 2016, (Due Wednesday, Nov. 23, 2016)**

1. A disk of radius  $a$  carrying a uniform surface charge density  $\sigma$  spins on its axis with an angular velocity  $\omega$ . Find the magnetic field  $B$  at a point  $z$  above the center of the disk as shown below.



2. Helmholtz coils. Two circular coils of radius  $R$ , each carrying current  $I$  in the same direction are parallel with  $xy$  plane with their center at  $(0,0, \pm s/2)$ .



- (a) On the  $z$ -axis, the magnetic field is a function of  $z$ ,  $\vec{B} = B(z)\hat{k}$ . Show that at  $z = 0$ , the first derivative of the field is equal to zero.  
 (b) Find the value of  $s$ , such that the second derivative of the  $B$  field with respect to  $z$  is also zero at  $z = 0$ .
3. A long copper rod carries a current density of  $J_0$  in the  $z$ -direction. The cross-section of the rod is shown below. The radius of the rod is  $R$  and there is a small circular cavity runs along the  $z$ -axis with its center at  $(a,0)$ , the radius of the cavity is  $b$ . Find the magnetic field at the center of the cavity  $(a, 0)$ .

