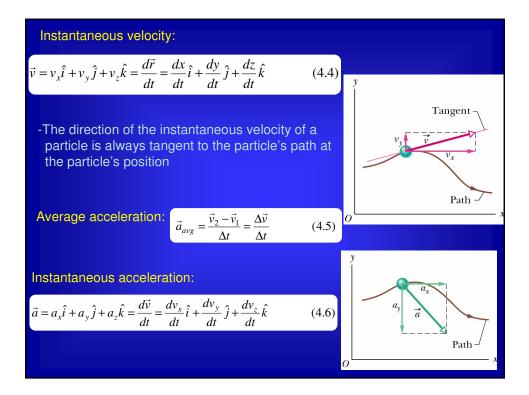
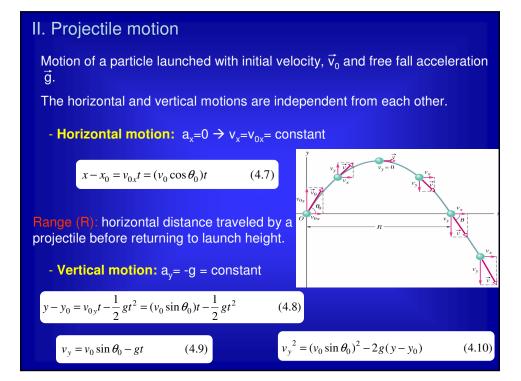


I. Definitions Position vector: extends from the origin of a coordinate system to the particle. $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ (4.1) Displacement vector: represents a particle's position change during a certain time interval. $\Delta \vec{r} = \vec{r}_2 - \vec{r}_1 = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}$ (4.2) Average velocity: $\vec{v}_{avg} = \frac{\Delta \vec{r}}{\Delta t} = \frac{\Delta x}{\Delta t}\hat{i} + \frac{\Delta y}{\Delta t}\hat{j} + \frac{\Delta z}{\Delta t}\hat{k}$ (4.3) Initial position Later Path of particle $\Delta \vec{r}$ position



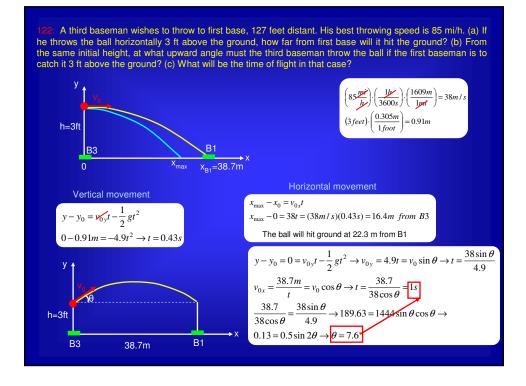


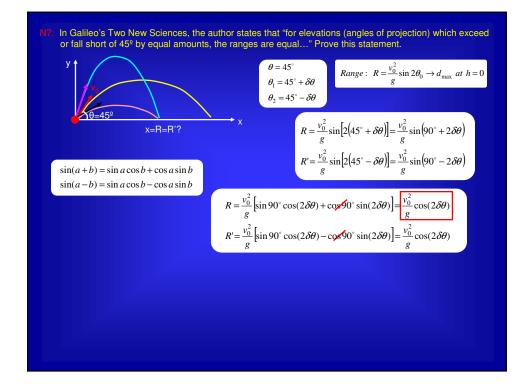
- Trajectory: projectile's path.
$$x_{0} = y_{0} = 0$$

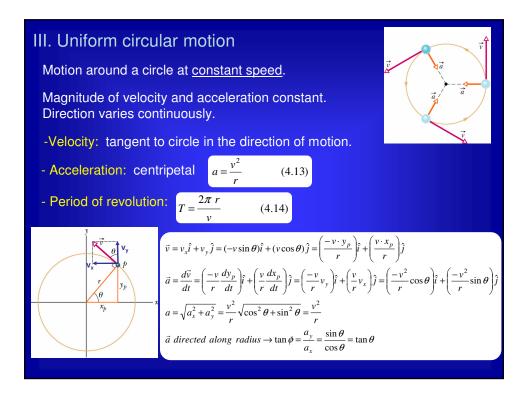
$$(4.7) + (4.8) \rightarrow t = \frac{x}{v_{0} \cos \theta_{0}} \rightarrow y = v_{0} \sin \theta_{0} \frac{x}{v_{0} \cos \theta_{0}} - \frac{1}{2} g \left(\frac{x}{v_{0} \cos \theta_{0}}\right)^{2} \rightarrow y = (\tan \theta_{0}) x - \frac{gx^{2}}{2(v_{0} \cos \theta_{0})^{2}} \qquad (4.11)$$
- Horizontal range: $R = x - x_{0}$; $y - y_{0} = 0$.
$$R = (v_{0} \cos \theta_{0})t \rightarrow t = \frac{R}{v_{0} \cos \theta_{0}}$$

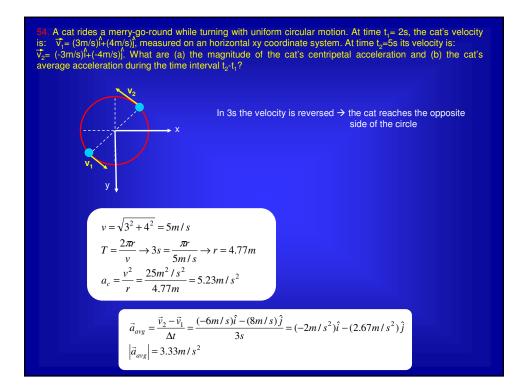
$$\theta = (v_{0} \sin \theta_{0})t - \frac{1}{2}gt^{2} = (v_{0} \sin \theta_{0})\frac{R}{v_{0} \cos \theta_{0}} - \frac{1}{2}g\left(\frac{R}{v_{0} \cos \theta_{0}}\right)^{2} = R \tan \theta_{0} - \frac{1}{2}g\frac{R^{2}}{v_{0}^{2} \cos^{2} \theta_{0}} \rightarrow$$

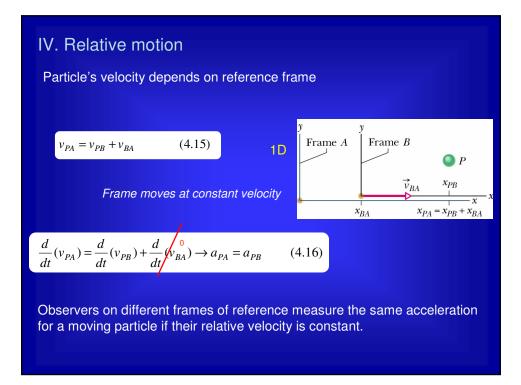
$$R = \frac{2\sin \theta_{0} \cos \theta_{0}}{g}v_{0}^{2} = \frac{v_{0}^{2}}{g} \sin 2\theta_{0} \qquad (4.12) \quad (Maximum for a launch angle of 45^{\circ})$$
Overall assumption: the air through which the projectile moves has no effect on its motion \rightarrow friction neglected.

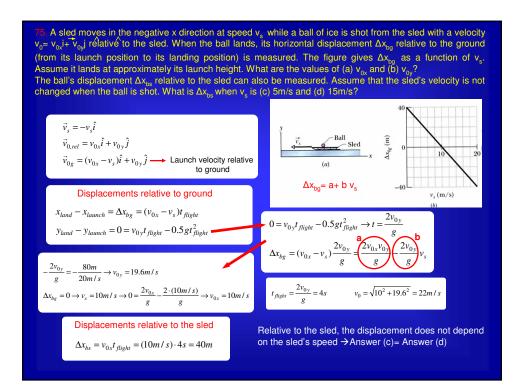


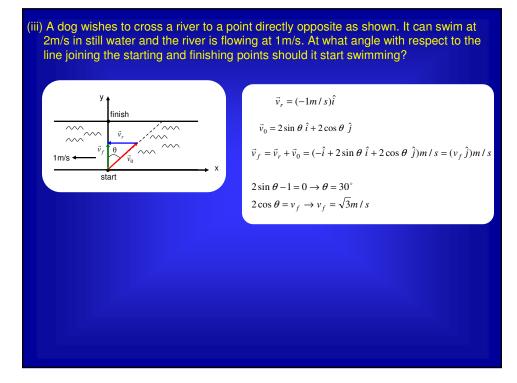












(ii) A particle moves with constant speed around the circle below. When it is at point A its coordinates are x=0, y=3m and its velocity is $(5m/s)^2$. What are its velocity and acceleration at point B? Express your answer in terms of unit vectors.

