Physics for Scientists and Engineers I

PHY 2048H

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Chapter 1 - Introduction

- I. General
- II. International System of Units
- III. Conversion of units
- IV. Dimensional Analysis
- V. Problem Solving Strategies

I. Objectives of Physics

- Find the limited number of fundamental laws that govern natural phenomena.
- Use these laws to develop theories that can predict the results of future experiments.
- -Express the laws in the language of mathematics.
- Physics is divided into six major areas:
 - 1. Classical Mechanics (PHY2048)
 - 2. Relativity
 - 3. Thermodynamics
 - 4. Electromagnetism (PHY2049)
 - 5. Optics (PHY2049)
 - 6. Quantum Mechanics

II. International System of Units

QUANTITY	UNIT NAME	UNIT SYMBOL
Length	meter	m
Time	second s	
Mass	kilogram	kg
Speed		m/s
Acceleration		m/s ²
Force	Newton	N
Pressure	Pascal	$Pa = N/m^2$
Energy	Joule	J = Nm
Power	Watt	W = J/s
Temperature	Kelvin	К

POWER	PREFIX	ABBREVIATION
1015	peta	Р
1012	tera	T
109	giga	G
106	mega	М
103	kilo	k
102	hecto	h
101	deka	da
10-1	deci	D
10-2	centi	С
10-3	milli	m
10-6	micro	μ
10-9	nano	n
10-12	pico	p
10-15	femto	f

III. Conversion of units

Chain-link conversion method: The original data are multiplied successively by conversion factors written as unity. Units can be treated like algebraic quantities that can cancel each other out.

Example: $316 \text{ feet/h} \rightarrow \text{m/s}$

$$\left(316 \frac{\text{feet}}{\text{K}}\right) \cdot \left(\frac{1 \text{ K}}{3600 \text{ s}}\right) \cdot \left(\frac{1 \text{ m}}{3.28 \text{ feet}}\right) = 0.027 \text{ m/s}$$

IV. Dimensional Analysis

Dimension of a quantity: indicates the type of quantity it is; length [L], mass [M], time [T]

Dimensional consistency: both sides of the equation must have the same dimensions.

Example: $x=x_0+v_0t+at^2/2$

$$[L] = [L] + \frac{[L]}{[V]}[V] + \frac{[L]}{[V^2]}[V^2] = [L] + [L] + [L]$$

Note: There are no dimensions for the constant (1/2)

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Units of Area, Volume, Velocity, Speed, and Acceleration					
System	Area (L^2)	Volume (L^3)	Speed (L/T)	Acceleration (L/T^2)	
SI	m^2	m ³	m/s	m/s^2	
	0.9	- 9	2.0	0 / 9	

ft

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U.S. customary

Significant figure → one that is reliably known.

ft⁴

Zeros may or may not be significant:

- Those used to position the decimal point are not significant.

ft/s

ft/s²

- To remove ambiguity, use scientific notation.

Ex: 2.56 m/s has 3 significant figures, 2 decimal places.

0.000256 m/s has 3 significant figures and 6 decimal places.

10.0 m has 3 significant figures.

1500 m is ambiguous \rightarrow 1.5 x 10³ (2 figures), 1.50 x 10³ (3 fig.),

1.500 x 10³ (4 figs.)

Order of magnitude → the power of 10 that applies.

V. Problem solving tactics

- Explain the problem with your own words.
- Make a good picture describing the problem.
- Write down the given data with their units. Convert all data into S.I. system.
- Identify the unknowns.
- Find the connections between the unknowns and the data.
- Write the physical equations that can be applied to the problem.
- Solve those equations.
- Always include units for every quantity. Carry the units through the entire calculation.
- Check if the values obtained are reasonable → order of magnitude and units.

MECHANICS → Kinematics

Chapter 2 - Motion along a straight line

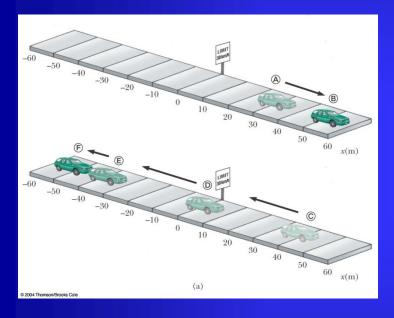
- I. Position and displacement
- II. Velocity
- III. Acceleration
- IV. Motion in one dimension with constant acceleration
- V. Free fall

Particle: point-like object that has a mass but infinitesimal size.

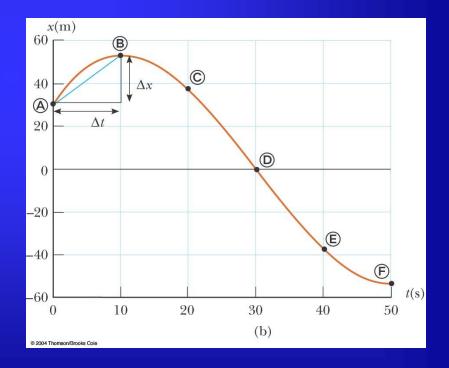
I. Position and displacement

Position: Defined in terms of a frame of reference: x or y axis in 1D.

- The object's position is its location with respect to the frame of reference.



Position-Time graph: shows the motion of the particle (car).

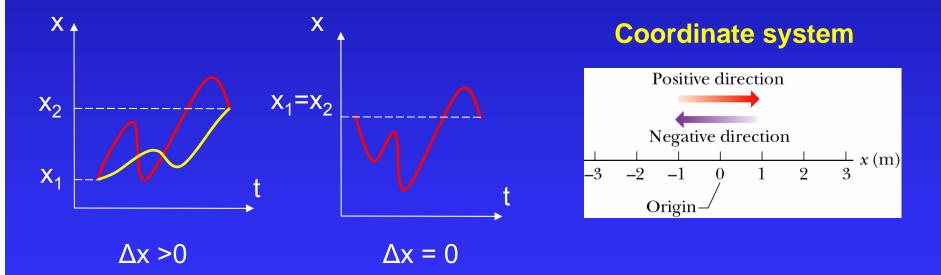


The smooth curve is a guess as to what happened between the data points.

I. Position and displacement

Displacement: Change from position x_1 to $x_2 \rightarrow \Delta x = x_2 - x_1$ (2.1) during a time interval.

- Vector quantity: Magnitude (absolute value) and direction (sign).
- Coordinate (position) \neq Displacement $\rightarrow x \neq \Delta x$



Only the initial and final coordinates influence the displacement \rightarrow many different motions between x_1 and x_2 give the same displacement.

Distance: length of a path followed by a particle.

- Scalar quantity

Displacement ≠ Distance

Example: round trip house-work-house → distance traveled = 10 km displacement = 0

Review:

- Vector quantities need both magnitude (size or numerical value) and direction to completely describe them.
- We will use + and signs to indicate vector directions in 1D motion.
- Scalar quantities are completely described by magnitude only.

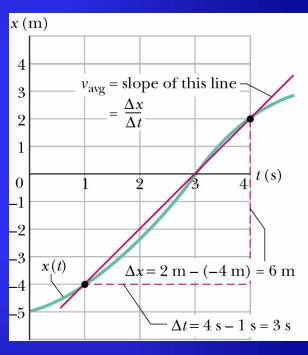
II. Velocity

Average velocity: Ratio of the displacement Δx that occurs during a particular time interval Δt to that interval.

$$v_{avg} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1}$$
 (2.2)

- -<u>Vector quantity</u> → indicates not just how fast an object is moving but also in which direction it is moving.
- SI Units: m/s
- Dimensions: Length/Time [L]/[T]
- The slope of a straight line connecting 2 points on an x-versus-t plot is equal to the <u>average velocity</u> during that time interval.

Motion along x-axis



Average speed: Total distance covered in a time interval.

$$S_{avg} = \frac{\text{Total distance}}{\Delta t}$$
 (2.3)

S_{avg} ≠ magnitude V_{avg}

S_{avg} always >0

Scalar quantity

Same units as velocity

Example: A person drives 4 mi at 30 mi/h and 4 mi and 50 mi/h → Is the average speed >,<,= 40 mi/h?

 t_1 = 4 mi/(30 mi/h)=0.13 h ; t_2 = 4 mi/(50 mi/h)=0.08 h \rightarrow t_{tot} = 0.213 h

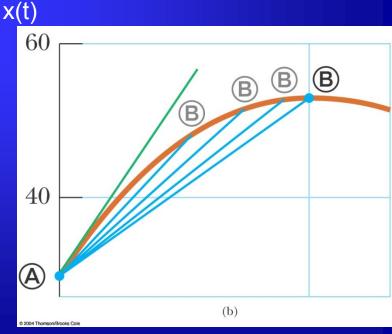
 \rightarrow S_{avg}= 8 mi/0.213h = 37.5mi/h

Instantaneous velocity: How fast a particle is moving at a given instant.

$$v_{x} = \lim_{\Delta t \to 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$
 (2.4)

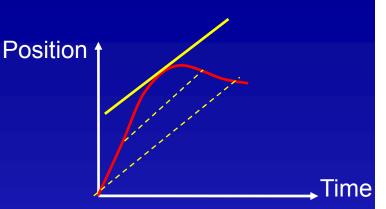
- Vector quantity

- The limit of the average velocity as the time interval becomes infinitesimally short, or as the time interval approaches zero.
- The instantaneous velocity indicates what is happening at every point of time.
- Can be positive, negative, or zero.
- The instantaneous velocity is the slope of the line tangent to the *x* vs. *t* curve at a given instant of time (green line).



Instantaneous velocity:

Slope of the particle's position-time curve at a given instant of time. V is tangent to x(t) when $\Delta t \rightarrow 0$



When the velocity is constant, the average velocity over any time interval is equal to the instantaneous velocity at any time.

Instantaneous speed: Magnitude of the instantaneous velocity.

Example: car speedometer.

- Scalar quantity

Average velocity (or average acceleration) always refers to an specific time interval.

Instantaneous velocity (acceleration) refers to an specific instant of time.

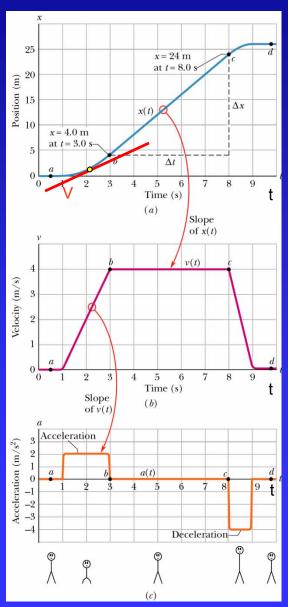
III. Acceleration

Average acceleration: Ratio of a change in velocity Δv to the time interval

Δt in which the change occurs.

$$a_{avg} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t}$$
 (2.5)

- Vector quantity
- Dimensions [L]/[T]², Units: m/s²
- The average acceleration in a "v-t" plot is the slope of a straight line connecting points corresponding to two different times.



Instantaneous acceleration: Limit of the average acceleration as Δt approaches zero.

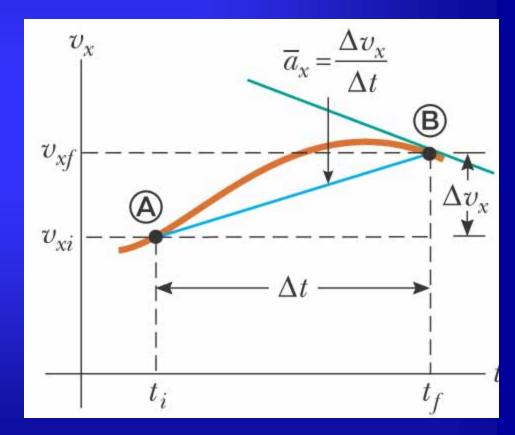
- <u>Vector quantity</u> $a = \lim_{\Delta t \to 0} \frac{\Delta v}{\Delta t} = \frac{dv}{dt} = \frac{d^2x}{dt^2}$ (2.6)

- The instantaneous acceleration is the slope of the tangent line (v-t plot) at

a particular time. (green line in B)

- Average acceleration: blue line.

- When an object's velocity and acceleration are in the same direction (same sign), the object is speeding up.
- When an object's velocity and acceleration are in the opposite direction, the object is slowing down.



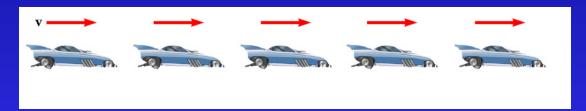
- Positive acceleration does not necessarily imply speeding up, and negative acceleration slowing down.

<u>Example (1):</u> $v_1 = -25 \text{m/s}$; $v_2 = 0 \text{m/s}$ in $5 \text{s} \rightarrow \text{particle slows down, } a_{avg} = 5 \text{m/s}^2$

- An object can have simultaneously v=0 and a≠0

Example (2): $x(t)=At^2 \rightarrow v(t)=2At \rightarrow a(t)=2A$; At t=0s, v(0)=0 but a(0)=2A

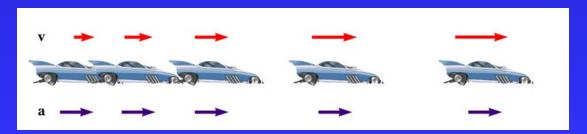
Example (3):



- The car is moving with constant positive velocity (red arrows maintaining same size) → Acceleration equals zero.

Example (4):

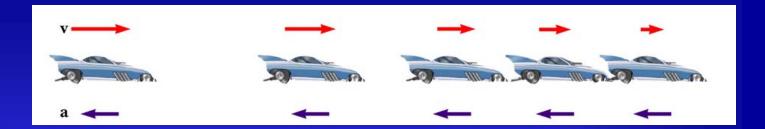
- + acceleration
- + velocity



- Velocity and acceleration are in the same direction, "a" is uniform (blue arrows of same length) → Velocity is increasing (red arrows are getting longer).

Example (5):

- acceleration
- + velocity



- Acceleration and velocity are in opposite directions.
- Acceleration is uniform (blue arrows same length).
- Velocity is decreasing (red arrows are getting shorter).

IV. Motion in one dimension with constant acceleration

- Average acceleration and instantaneous acceleration are equal.

$$a = a_{avg} = \frac{v - v_0}{t - 0}$$

- Equations of motion with constant acceleration:

$$v = v_0 + at$$

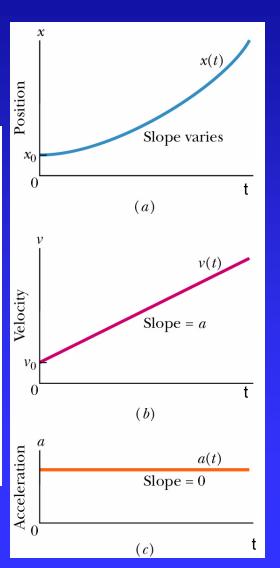
$$v_{avg} = \frac{x - x_0}{t} \rightarrow x = x_0 + v_{avg}t \qquad (2.8)$$

$$v_{avg} = \frac{v_0 + v}{2} \quad and \quad (2.7) \rightarrow v_{avg} = v_0 + \frac{at}{2} \qquad (2.9)$$

$$(2.8), (2.9) \rightarrow x - x_0 = v_0 t + \frac{at^2}{2} \qquad (2.10)$$

$$(2.7), (2.10) \rightarrow v^2 = v_0^2 + a^2 t^2 + 2a(v_0 t) = v_0^2 + a^2 t^2 + 2a(x - x_0 - \frac{at^2}{2})$$

$$\rightarrow v^2 = v_0^2 + 2a(x - x_0) \qquad (2.11)$$
t missing

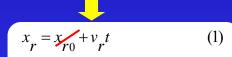


PROBLEMS - Chapter 2

P1. A red car and a green car move toward each other in adjacent lanes and parallel to The x-axis. At time t=0, the red car is at x=0 and the green car at x=220 m. If the red car has a constant velocity of 20km/h, the cars pass each other at x=44.5 m, and if it has a constant velocity of 40 km/h, they pass each other at x=76.6m. What are (a) the initial velocity, and (b) the acceleration of the green car?



$$\left(40\frac{km}{h}\right) \cdot \left(\frac{1h}{3600s}\right) \cdot \left(\frac{10^3 m}{1km}\right) = 11.11 m/s$$



$$x_g = x_{g0} + v_{g0}t + \frac{1}{2}at^2 \tag{2}$$



$$x_{r1} = v_{r1}t_1 \to t_1 = \frac{44.5m}{5.55m/s} = 8s$$

$$x_{r2} = v_{r2}t_2 \to t_2 = \frac{76.6m}{11.11m/s} = 6.9s$$

$$x_{r2} - x_g = \exists v_{g0} t_2 \exists 0.5 \cdot a_g t_2^2 \to 76.6 - 220 = -v_{g0} \cdot (6.9s) - 0.5 \cdot (6.9s)^2 a_g$$

$$x_{r1} - x_g = \exists v_{g0} t_1 \exists 0.5 \cdot a_g t_1^2 \to 44.5 - 220 = -v_{g0} \cdot (8s) - 0.5 \cdot (8s)^2 a_g$$

The car moves to the left (-) in my reference system → a<0, v<0

$$a_g = 2.1 \text{ m/s}^2$$

 $v_{0g} = 13.55 \text{ m/sc}$

P2: At the instant the traffic light turns green, an automobile starts with a constant acceleration a of 2.2 m/s². At the same instant, a truck, traveling with constant speed of 9.5 m/s, overtakes and passes the automobile. (a) How far beyond the traffic signal will the automobile overtake the truck? (b) How fast will the automobile be traveling at that instant?

$$x_{T} = d = v_{T}t = 9.5 \ t \rightarrow (1)$$
 Truck
$$(a) \ 9.5 \cdot t = 1.1 \cdot t^{2} \rightarrow t = 8.63 \ s \rightarrow d = (9.5m/s)(8.63s) \approx 82m$$

$$x_{C} = d = v_{C0}t + \frac{1}{2}a_{C}t^{2} \rightarrow d = 0 + 0.5 \cdot (2.2m/s^{2}) \cdot t^{2} = 1.1t^{2}$$
 (2) Car
$$(b) \ v_{f}^{2} = v_{0}^{2} + 2 \cdot a_{C} \cdot d = 2 \cdot (2.2m/s^{2}) \cdot (82m) \rightarrow v_{f} = 19m/s$$

(a)
$$9.5 \cdot t = 1.1 \cdot t^2 \rightarrow t = 8.63 \ s \rightarrow d = (9.5m/s)(8.63s) \approx 82m$$

(b)
$$v_f^2 = v_0^2 + 2 \cdot a_c \cdot d = 2 \cdot (2.2m/s^2) \cdot (82m) \rightarrow v_f = 19m/s$$

P3: A proton moves along the x-axis according to the equation: $x = 50t + 10t^2$, where x is in meters and t is in seconds. Calculate (a) the average velocity of the proton during the first 3s of its motion.

$$v_{\text{avg}} = \frac{x(3) - x(0)}{\Delta t} = \frac{(50)(3) + (10)(3)^2 - 0}{3} = 80 \text{ m/s}.$$

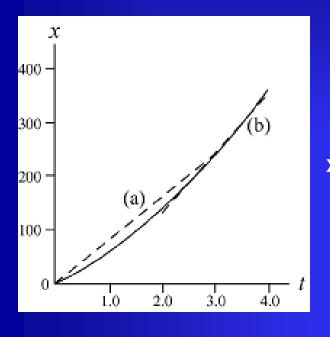
(b) Instantaneous velocity of the proton at t = 3s.

$$v(t) = \frac{dx}{dt} = 50 + 20 \ t \rightarrow v(3s) = 50 + 20 \cdot 3 = 110 \ m/s$$

(c) Instantaneous acceleration of the proton at t = 3s.

$$a(t) = \frac{dv}{dt} = 20 \ m/s^2 = a(3s)$$

(d) Graph x versus t and indicate how the answer to (a) (average velocity) can be obtained from the plot.



- (e) Indicate the answer to (b) (instantaneous velocity) on the graph.
- (f) Plot v versus t and indicate on it the answer to (c).

$$x = 50t + 10t^{2}$$

$$150 - 10$$

P4. An electron moving along the x-axis has a position given by: $x = 16t \cdot exp(-t)$ m, where t is in seconds. How far is the electron from the origin when it momentarily stops?

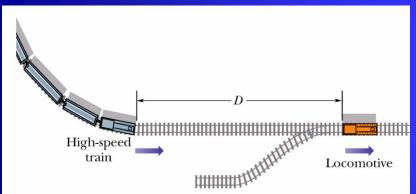
x(t) when v(t)=0??

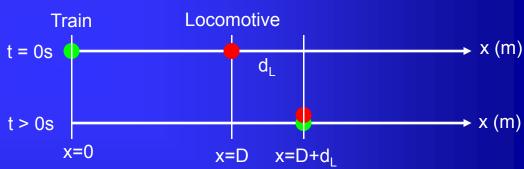
$$\frac{dx}{dt} = v = 16e^{-t} - 16te^{-t} = 16e^{-t}(1-t)$$

$$v = 0 \to (1-t) = 0; \ (e^{-t} > 0) \to t = 1s$$

$$x(1) = 16/e = 5.9m$$

When a high speed passenger train traveling at 161 km/h rounds a bend, the engineer is shocked to see that a locomotive has improperly entered into the track from a siding and is a distance D= 676 m ahead. The locomotive is moving at 29 km/h. The engineer of the high speed train immediately applies the brakes. (a) What must be the magnitude of the resultant deceleration if a collision is to be avoided? (b) Assume that the engineer is at x=0 when at t=0 he first spots the locomotive. Sketch x(t) curves representing the locomotive and high speed train for the situation in which a collision is just avoided and is not quite avoided.





 v_T =161km/h = 44.72 m/s = $v_{T0} \rightarrow$ 1D movement with a<0=cte

 v_L =29 km/h = 8.05 m/s is constant

$$d_L = v_L t = 8.05 \ t \rightarrow t = \frac{d_L}{8.05}$$
 (1) Locomotive
$$d_L + D = v_{T0} t + \frac{1}{2} a_T t^2 \rightarrow d_L + 676 = 44.72 \ t + \frac{1}{2} a_T t^2$$
 (2) Train

$$v_{Tf} = v_{T0} + a_T t = 0 \rightarrow a_T = \frac{-44.72m/s}{t} = (eq. \ 1) = \frac{(-44.72m/s)(8.05m/s)}{d_L} = \frac{-360m^2/s^2}{d_L}$$

$$v_{Tf}^2 = v_{T0}^2 + 2a_T(D + d_L) = 0 \rightarrow a_T = \frac{-(44.72m/s)^2}{2(676m + d_L)}$$

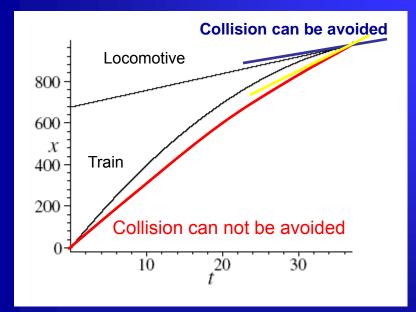
$$(3) = (4) \rightarrow d_L = 380.3m$$

$$(4)$$

$$\Rightarrow$$

from (1)
$$\rightarrow t = \frac{d_L}{8.05} = 47.24s$$

(1) + (3) $\rightarrow a_T = \frac{-360m^2/s^2}{380.3m} = \frac{-0.947m/s^2}{10.947m}$



$$x_L = 676 + 8.05 t$$

 $x_T = 44.72 t + 0.5 a_T t^2$

- Collision can be avoided:

Slope of x(t) vs. t locomotive at t = 47.24 s (the point were both Lines meet) = v instantaneous locom > Slope of x(t) vs. t train

- Collision cannot be avoided:

Slope of x(t) vs. t locomotive at t = 47.24 s < Slope of x(t) vs. t train

- The motion equations can also be obtained by indefinite integration:

$$dv = a \ dt \to \int dv = \int a \ dt \to v = at + C; \qquad v = v_0 \quad at \quad t = 0 \to v_0 = (a)(0) + C \to v_0 = C \to v = v_0 + at$$

$$dx = v \ dt \to \int dx = \int v \ dt \to \int dx = \int (v_0 + at) dt \to \int dx = v_0 \int dt + a \int t \ dt \to x = v_0 t + \frac{1}{2} a t^2 + C';$$

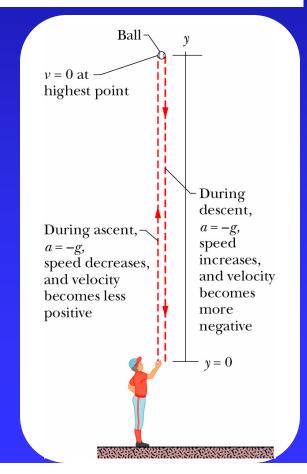
$$x = x_0 \quad at \quad t = 0 \to x_0 = v_0(0) + \frac{1}{2} a(0) + C' \to x_0 = C' \to x = x_0 + v_0 t + \frac{1}{2} a t^2$$

V. Free fall

Motion direction along y-axis (y >0 upwards)

Free fall acceleration: (near Earth's surface) a= -g = -9.8 m/s² (in mov. eqs. with constant acceleration)

Due to gravity → downward on y, directed toward Earth's center



Approximations:

- Locally, Earth's surface essentially flat → free fall "a" has same direction at slightly different points.
- All objects at the same place have same free fall "a" (neglecting air influence).

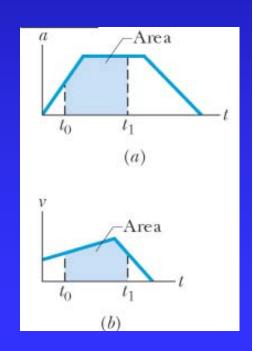
VI. Graphical integration in motion analysis

From a(t) versus t graph \rightarrow integration = area between acceleration curve and time axis, from t_0 to $t_1 \rightarrow v(t)$

$$v_1 - v_0 = \int_{t_0}^{t_1} a \cdot dt$$

Similarly, from v(t) versus t graph \rightarrow integration = area under curve from t₀ to t₁ \rightarrow x(t)

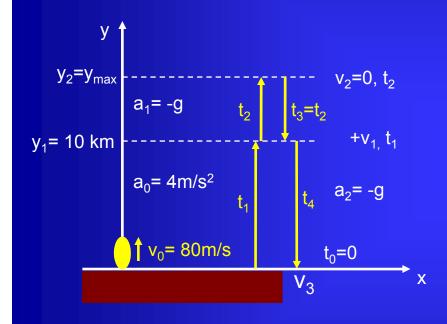
$$x_1 - x_0 = \int_{t_0}^{t_1} v \cdot dt$$



P6: A rocket is launched vertically from the ground with an initial velocity of 80m/s. It ascends with a constant acceleration of 4 m/s² to an altitude of 10 km. Its motors then fail, and the rocket continues upward as a free fall particle and then falls back down.

- (a) What is the total time elapsed from takeoff until the rocket strikes the ground?
- (b) What is the maximum altitude reached?
- (c) What is the velocity just before hitting ground?

1) Ascent $\rightarrow a_0 = 4 \text{m/s}^2$



$$y_1 - y_0 = v_0 t_1 + 0.5 \cdot a_0 t_1^2 \rightarrow 10^4 = 80t_1 + 2t_1^2 \rightarrow t_1 = 53.48s$$

$$a_0 = \frac{v_1 - v_0}{t_1} \rightarrow v_1 = (4m/s^2) \cdot (53.48s) + 80m/s = 294m/s$$

2) Ascent \rightarrow a= -9.8 m/s²

$$a_1 = -g = \frac{0 - v_1}{t_2} \rightarrow t_2 = \frac{-294m/s}{-9.8m/s^2} = 29.96s$$

Total time ascent = t_1+t_2 = 53.48 s+29.96 s= 83.44 s

3) Descent \rightarrow a= -9.8 m/s²

$$0 - y_1 = -v_1 t_4 + 0.5 \cdot a_0 t_4^2 \rightarrow -10^4 = -294 t_4 - 4.9 t_4^2 \rightarrow t_4 = 24.22 s$$

$$t_{\text{total}} = t_1 + 2t_2 + t_4 = 53.48 \text{ s} + 2.29.96 \text{ s} + 24.22 \text{ s} = 137.62 \text{ s}$$

$$h_{max} = y_2 \rightarrow y_2 - 10^4 \text{ m} = v_1 t_2 - 4.9 t_2^2 = (294 \text{ m/s})(29.96 \text{s}) - (4.9 \text{ m/s}^2)(29.96 \text{s})^2 = 4410 \text{ m} \rightarrow h_{max} = 14.4 \text{ km}$$

$$a_2 = -g = \frac{v_3 - (-v_1)}{t_4} \rightarrow v_3 = -g \cdot t_4 - v_1 = -531.35 m/s$$